### **TECHNICAL SCIENCES**

## *Lahutin V.L.* Mathematical model of flat vertical oscillations of the trolley for transporting dangerous cargo with usage of pneumatic elements in the second stage of suspension

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Abstract. We are introducing the construction of a mathematical model of plane vertical oscillations of the trolley for transporting dangerous cargo, which has a two-stage spring suspension using high quality pneumatic elements.

Keywords: explosive cargo, two stage spring suspension, vibrations.

*Statement of the problem.* For transportation of dangerous, particularly explosive cargo from a location to the point of utilization it was designed the construction of a special trolley [1], which spring suspension has characteristics that satisfy the requirements for safe transportation, and absence of an engine and transmission makes a simple and reliable design of the construction (Fig. 1).



Fig. 1. – Schematic design of the vehicle. 1 – load platform,
2 – the air one-ridged shell 3 – support platform, 4 – turntable
platform, 5 – elastic elements of the first stage of suspension, 6
– wheels of trolley, 7 – profile of the road.

The main feature of the design of the trolley, as opposed to the traditional for automobile manufacturing single spring suspension, is the usage of the additional second stage with the stiffness corrector [2-4], the dynamic characteristics of which provide conditions for safe transportation.

Some features of this design [5] in a real operation that may significantly complicate preparations for the transport of dangerous cargo are solved using canned oneridged elastic elements [6] in reference points of the load platform and the described turntable platform of the first axis bound significantly improves driving performance of the trolley, especially on curved sections of roads.

Determination of the required parameters of the introduced spring suspension, which is strongly dependent on its dynamic properties, estimates should be provided on a mathematical model of plane vertical oscillations of the described design.

Analysis of recent research and publications. General theoretical foundations of mathematical models and calculation methods of spring suspension of modern vehicles are set out in the work [7-10], and the design of mathematical models of the trolley for transportation of dangerous cargo with different constructions of elastic elements in the second stage in the works [11-12].

Calculation of thermodynamic processes within designing of the air spring suspension system paths, based on the theory of "filling-emptying" and the quasistationary method of determining the parameters of the the air condition that are reviewed in the works [13-15].

Statement of the problem and its solution. Keeping in mind that the vertical oscillations in the longitudinal plane are the main influence on the dynamic properties of the transport system it is appropriate to perform their calculation on two-axis model (Fig. 2).

To construct an appropriate mathematical model trolley is considered as a system involving four elasticconnected solid bodies:

- load platform with cargo and brought it to the weight of the second stage spring suspension, which is denoted by the weight  $M_2$ ;

- support platform with reduced her weight by parts of the second and first stage spring suspension, a lot of which is denoted by  $M_l$ ;

- trolley wheels, dual weight are denoted by  $M_{01}$  and  $M_{02}$ .

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**Fig. 2.** – The flat vertical mechanical model of the trolley.  $M_2$  – weight load platform,  $C_2^{e_{RR}}$  – equivalent stiffness of the elastic element of the second stage,  $M_1$  – weight of the support platform,  $C_1$ -stiffness of torsions of the first stage of suspension,  $R_1$ 

- viscous friction in the suspension of the first stage,  $M_0$  - weight of the trolley wheels,  $C_0$  - the equivalent stiffness of

tires,  $R_0$  – viscous friction in tires,  $\eta$  – profile of the road.

Scheme of the modified elastic element of the second stage pneumatic suspension with corrector stiffness in the transverse plane is shown on the Figure 3.

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**Fig. 3.** – Scheme of the modified elastic element of the second stage of the pneumatic suspension with stiffness corrector. 1 – load floor, 2 – rubber-cord one-ridged shell 3 – throttling orifice, 4 – extra tank, 5 – support platform 6 – stiffness corrector springs.

During creating the mathematical model it is decided to use absolute and local coordinate systems (Fig.4).

Fixed an absolute coordinate system  $\zeta G \zeta$  located at the beginning of the trajectory, where the center of weight of the load platform in the absence of involuntary movements.

The local coordinate systems *XOZ* (indexes) are associated with the centers of weight of corresponding solids meet their fluctuations relative to the provisions of the static equilibrium and moving relative to the absolute coordinate system  $\xi G \zeta$  with the constant speed *V*.

Thus, the vertical plane vibrations of the introduced mechanical system are defined by the following coordinates:

- Vertical movement of the load platform  $-Z_2$ ;

- Vertical movement of the support platform  $-Z_l$ ;

- Angle of the load platform in the longitudinal plane –  $\varphi_2$ ;

- Angle of the support platform in the longitudinal plane  $-\varphi_i$ :

- Vertical movement of the trolley wheels  $-Z_{01}$  and  $Z_{02}$ .

Longitudinal motion of the system is determined by the equation

$$H01 = H02 = X1 = X2 = X = Vt, (1)$$

where V – velocity, t – time.

Considering the much larger compared to the stiffness of rubber tires road surface as the causative agent of powerd oscillations of the trolley it is taken an absolutely rigid geometric profile of the given configuration  $\eta = \eta$  ( $\xi$ ).

Dual tire stiffness is denoted by  $C_0$ .

In the first stage of the spring suspension of the given vehicle it is taken the traditional for automobile manufacturing independent torsion suspension of each of the four trolley wheels. Dual torsion stiffness denoted  $C_l$ .



Fig. 4. – Absolute and local coordinate systems.

The second stage of the spring suspension, which is consisted of four elastic pneumatic elements and two stiffness correctors, is simulated using research results posted in earlier works [18-20].

The total stiffness of the corrector springs is denoted by  $C_2$ , their length in the static position – L, and the initial deformation –  $\delta$ .

Analysis of the structural features of the second stage of spring suspension showed that the volume of the air pipe is much smaller than the other components of pneumatic system that eliminates it from the mathematical model of the process [16].

In view of the above, the differential equations of motion of the trolley oscillatory processes consist of static equilibrium with respect to the provisions of relevant weightes using the general provisions of the speakers.

The following groups of equations are used for the mathematical model:

- kinetostatics equation for the elements of the mechanical system;

- geometric dependencies that determine the relative position and movement of the mechanical elements of the system;

- analytical and experimental characteristics of elastic elements of the mechanical system;

- thermodynamic equations that define the processes in the system pneumatic spring suspension.

Powers that influence the components of the mechanical model of the trolley shown on Figures 5 and 6.

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**Fig. 5.** – Powers that influence the components of the mechanical model of the trolley in the longitudinal plane.  $M_2$  – weight of the load platform,  $F^{II}_{21}$ ,  $F^{II}_{22}$  – the powers in the elements of the second degree hanging,  $M_1$  – weight of the support platform,  $F_{11}$ ,  $F_{12}$  – elastic power in the first stage of suspension,  $R_{11}$ ,  $R_{12}$  – dissipative powers in the first stage spring suspension,  $M_{01}$ ,  $M_{02}$  – weight of the trolley wheels,  $F_{01}$ ,  $F_{02}$ – powers of the elastic tires,  $R_{01}$ ,  $R_{02}$  – dissipative powers in the tires.



Fig. 6. – Powers that influence elements of the second stage of spring suspension of the trolley in the transverse plane.  $M_2$  – weight of the load platform,  $F_{\Pi}$  – double power in the second

stage pneumatic elements,  $F_K$  – power springs corrector stiffness in the second stage,  $M_1$  – weight of the support platform.

The elastic powers  $-F_{0P}F_{1P}F_{02}F_{12}$ , acting on the tires and torsion suspension equal to the first stage

$$F_{01} = C_0 \varDelta_{01}, \ F_{11} = C_1 \varDelta_{11}, \ F_{02} = C_0 \varDelta_{02}, \ F_{12} = C_1 \varDelta_{12}, \ (2)$$

where:  $\Delta_{0l}, \Delta_{ll}, \Delta_{02}, \Delta_{l2}$  – deformation of elastic elements constitute

> $\Delta_{01} = \eta_1 - Z_{01}, \ \Delta_{11} = Z_{01} - Z_1 + \varphi_1 a,$  $\Delta_{02} = \eta_2 - Z_{02}, \ \Delta_{12} = Z_{02} - Z_1 - \varphi_1 a.$ (3)

The elastic powers  $F_{21}^{\Pi}, F_{22}^{\Pi}$  of the second stage of suspension should be determined by the powers  $F_{\Pi I}, F_{\Pi 2}, F_{KI}, F_{K2}$ , respectively, pneumatic elements and spring stiffness corrections.

These powers are equal

 $F_{\Pi I} = P_{\Pi I} S_{\Pi I},$ in the pneumatic springs  $F_{\Pi 2} = P_{\Pi 2} S_{\Pi 2}, (4)$ 

in the correctors 
$$F_{KI} = C_2 \left( L + \delta - \sqrt{L^2 + \Delta_{21}^2} \right)$$
  
 $F_{K2} = C_2 \left( L + \delta - \sqrt{L^2 + \Delta_{22}^2} \right)$  (5)

where  $P_{\Pi I}, P_{\Pi 2}$  – excess pressure caused by thermodynamic processes in pneumatic membranes and determined decision of the appropriate equations,

 $S_{\Pi I}, S_{\Pi 2}$  – effective area of pneumatic membranes, depending on their working height is determined experimentally and is introduced into the equation mathematical model geometric dependencies

$$S_{\Pi I} = f(\Delta_{21}), \ S_{\Pi 2} = f(\Delta_{22})$$
(6)

where  $\Delta_{21}$ ,  $\Delta_{22}$  – deformations of pneumatic springs

 $\Delta_{21} = Z_1 - Z_2 - \varphi_1 a + \varphi_2 b, \ \Delta_{22} = Z_1 - Z_2 + \varphi_1 a - \varphi_2 b. \ (7)$ 

Dissipative powers in tires and first stage of suspension are modeled by viscous friction, which is proportional to the relative velocity corresponding elements

$$R_{01} = k_0 \dot{\Delta}_{01}, R_{02} = k_0 \dot{\Delta}_{02}, R_{11} = k_1 \dot{\Delta}_{11}$$
$$R_{11} = k_1 \dot{\Delta}_{12}$$

where:  $k_0$ ,  $k_1$  – binary viscous friction coefficient, respectively, in tires and torsion,

 $\Delta_{01}, \Delta_{02}, \Delta_{11}, \Delta_{12}, -$  corresponding relative velocities:

$$\dot{\Delta}_{01} = \dot{\eta}_1 - \dot{Z}_{01}, \ \dot{\Delta}_{11} = \dot{Z}_{01} - \dot{Z}_1 + \dot{\phi}_1 a, \dot{\Delta}_{02} = \dot{\eta}_2 - \dot{Z}_{02}, \ \dot{\Delta}_{12} = \dot{Z}_{02} - \dot{Z}_1 - \dot{\phi}_1 a.$$
<sup>(9)</sup>

Dissipative powers in the second stage pneumatic elements hanging defined energy dissipation in flowing the air from one volume to another through the throttling orifice with square hole  $S_D$  and defined and included in the appropriate thermodynamic equations.

Differential equations of motion oscillatory processes trolley consisting given above according to the distribution of elastic and dissipative powers four-weight model (Fig. 4-6).

For the wheels of the trolley

$$M_{o1}\ddot{Z}_{o1} = F_{o1} - F_{11} + R_{o1} - R_{11}, (10)$$
  

$$M_{o2}\ddot{Z}_{o2} = F_{o2} - F_{12} + R_{o2} - R_{12}. (11)$$
  
For the support platform

$$M_{I}\ddot{Z}_{I} = F_{II} + F_{I2} + R_{II} + R_{I2} - F_{2I}^{II} - F_{22}^{II}, (12)$$
  

$$I_{I}\ddot{\varphi}_{I} = -F_{II}a + F_{I2}a - R_{II}a + R_{I2}a + F_{2I}^{II}b - F_{22}^{II}b, (13)$$
  
or after the appropriate transformations

 $M_{1}\ddot{Z}_{1} = F_{11} + F_{12} + R_{11} + R_{12} - F_{111} - F_{112} - F_{K1}(sin\frac{\Delta_{21}}{I})sign\Delta_{21} - F_{K2}(sin\frac{\Delta_{22}}{I})sign\Delta_{22},$ (14)

$$I_{1}\ddot{\phi}_{1} = -F_{11}a + F_{12}a - R_{11}a + R_{12}a + F_{111}b - F_{12}b + F_{K1}b(\sin\frac{\Delta_{21}}{L})sign\Delta_{21} - F_{K2}b(\sin\frac{\Delta_{22}}{L})sign\Delta_{22}$$
(15)

For the load platform

$$M_{2}\ddot{Z}_{2} = F_{III} + F_{II2} + F_{KI}(\sin\frac{\Delta_{21}}{L})sign\Delta_{21} + F_{K2}(\sin\frac{\Delta_{22}}{L})sign\Delta_{22} - M_{2}g,$$
(16)  
$$I_{2}\ddot{\varphi}_{2} = -F_{III}b + F_{II2}b - F_{KI}b(\sin\frac{\Delta_{21}}{L})sign\Delta_{21} + F_{K2}b(\sin\frac{\Delta_{22}}{L})sign\Delta_{22},$$
(17)

where:  $I_1, I_2$  – given moments of inertia, respectively trucks and support platforms, 2a – wheelbase of the trolley, 2b – the distance between the the air castors of the load platform.

When creating the mathematical model of the thermodynamic processes in the pneumatic spring suspension of the trolley it was decided to use the results of earlier works [17], under which condition of the the air in each of the respective volumes two-element system (Fig. 7), is characterized by the following parameters: P pressure, T – temperature, G – weight, V – volume,  $\rho$  – density,  $C_p$  – specific heat of the air during *P*-const,  $C_v$  heat the the air in the process V - const, R - gas constant.



Fig. 7. – Diagram of pneumatic elements of the second stage of suspension. 1 - rubber-cord shell, 2 - the additional tank, 3 -

throttling orifice,  $S_D$  – Square hole throttling orifice,  $H_1$  – surface area rubber-cord shell  $H_2$  – additional surface area of the tank

Additional geometric parameters of pneumatic:  $H_1$  – surface area rubber-cord shell,  $H_2$  – additional surface area of the tank,  $S_D$  – Square hole throttling orifice.

A mathematical model of the thermodynamic process in the compression stroke the air springs in which the pressure in them more than additional tanks, i.e. with  $P_{\Pi I} > P_{AI}$  and  $P_{\Pi 2} > P_{A2}$ , is determined by the following system of equations.

Element 1.  $P_{\Pi l} > P_{\Pi l}$ 

Pneumatic spring:

- the amount of the air flowing through the throttling orifice with The air in an additional tank

$$dG_{\Pi I} \cong -\mu S_D \sqrt{2\rho_{\Pi I}} (P_{\Pi I} - P_{\mathcal{A}I}) dt , (18)$$

- the law of energy storage

$$RT_{III}dG_{III} - k_{I}H_{I}(T_{III} - T_{0})dt - C_{V}G_{III}dT_{III} - P_{III}dV_{III} = 0$$
(19)

- the equation of state of the air

$$P_{\Pi I}dV_{\Pi I} + V_{\Pi I}dP_{\Pi I} - RT_{\Pi I}dG_{\Pi I} - RG_{\Pi I}dT_{\Pi I} = 0.$$
(20)

The internal volume of the pneumatic membrane depends on its working height is determined experimentally and is introduced into the equation mathematical model geometry dependence

 $V_{\Pi l} = f(\varDelta_{2l}), (21)$ 

which enables every step solution of differential equations of the mathematical model to determine the  $dV_{\pi l}$ .

Additional tank:

Note that for an additional tank at  $V_{III} = const$ ,

 $dV_{II} = 0$ .

- the weight balance equation

 $dG_{III} + dG_{ZI} = 0$ , also  $dG_{ZI} = -dG_{III}$ , (22)

- the law of energy storage

$$C_{v}T_{\mu}dG_{\mu}-C_{v}T_{\mu}dG_{\mu}-RT_{\mu}dG_{\mu}-k_{2}H_{2}(T_{\mu}-T_{0})dt-C_{v}G_{\mu}dT_{\mu}=0,$$
(23)

- the equation of state of the air

 $V_{\mathcal{A}I}dP_{\mathcal{A}I} + RT_{\mathcal{A}I}dG_{\mathcal{A}I} - RG_{\mathcal{A}I}dT_{\mathcal{A}I} = 0, (24)$ Element 2.  $P_{\Pi 2} > P_{\Pi 2}$ Pneumatic spring:

- the amount of the air flowing through the throttling

orifice with the air in an additional tank  $C \sqrt{2} \sqrt{D}$ D 1 1 (25)

$$aG_{II2} \cong -\mu S_D \sqrt{2\rho_{II2}} (P_{II2} - P_{I2}) dt, (23)$$
- the law of energy storage  

$$RT_{II2} dG_{II2} - k_1 H_1 (T_{II2} - T_0) dt - C_V G_{II2} dT_{II2} - P_{II2} dV_{II2} = 0, (26)$$
- the equation of state of the air

 $P_{\Pi 2}dV_{\Pi 2} + V_{\Pi 2}dP_{\Pi 2} - RT_{\Pi 2}dG_{\Pi 2} - RG_{\Pi 2}dT_{\Pi 2} = 0, (27)$ 

The internal volume of the pneumatic membrane depends on its working height is determined experimentally and is introduced into the equation mathematical model geometry dependence

 $V_{II2} = f(\Delta_{22}), (28)$ 

which enables every step solution of differential equations of the mathematical model to determine the  $dV_{\Pi 2}$ .

Additional tank:

Note that for an additional tank at  $V_{JI2} = const$ ,

 $dV_{D2} = 0$ .

- the weight balance equation

$$dG_{\Pi 2} + dG_{\Lambda 2} = 0$$
, and  $dG_{\Lambda 2} = -dG_{\Pi 2}$  (29)

- the law of energy storage  $C_{v}T_{J2}dG_{J12} - C_{v}T_{J12}dG_{J12} - RT_{J12}dG_{J12} - k_{2}H_{2}(T_{J12} - T_{0})dt - C_{v}G_{J12}dT_{J12} = 0$ ,(30)

- the equation of state of the air

 $V_{J2}dP_{J2} + RT_{J2}dG_{J2} - RG_{J2}dT_{J2} = 0, (31)$ 

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Similarly (mutatis mutandis signs and direction of the air flow) are based equations defining enlargement beat The air pressure at which it is less than the extra tank, ie at  $P_{\Pi I} < P_{\Pi I}$  and  $P_{\Pi 2} < P_{\Pi 2}$ .

Element 1.  $P_{\Pi l} < P_{\Pi l}$ 

Pneumatic spring:

- the amount of the air flowing through the throttling orifice with extra tanks in the air

= 0

$$dG_{III} \cong +\mu S_D \sqrt{2\rho_{AI}} \left( P_{AI} - P_{III} \right) dt , (32)$$
  
- the law of energy storage  
$$RT_{AI} dG_{III} - k_1 H_1 (T_{III} - T_0) dt - C_V G_{III} dT_{III} - P_{III} dV_{III} - C_V T_{III} dG_{III} + C_V T_{AI} dG_{III} dG_{III} + C_V T_{AI} dG_{III} dG_{III} + C_V T_{AI} dG_{III} dG_{III} dG_{III} + C_V T_{AI} dG_{III} dG_{III$$

(33)

- the equation of state of the air

$$P_{\Pi I} dV_{\Pi I} + V_{\Pi I} dP_{\Pi I} - RT_{\Pi I} dG_{\Pi I} - RG_{\Pi I} dT_{\Pi I} = 0.$$
(34)  
Additional tank:

- the weight balance equation

$$dG_1 + dG_2 = 0$$
, (35) abo  $dG_{JI} = -dG_{III}$ , (36)

- the law of energy storage  

$$RT_{\mathcal{A}l}dG_{\mathcal{A}l} - C_V G_{\mathcal{A}l}dT_{\mathcal{A}l} - k_2 H_2 (T_{\mathcal{A}l} - T_0)dt = 0, (37)$$

- the equation of state of the air

$$V_{\mathcal{A}l} dP_{\mathcal{A}l} - RT_{\mathcal{A}l} dG_{\mathcal{A}l} - RG_{\mathcal{A}l} dT_{\mathcal{A}l} = 0. (38)$$
  
Element 2.  $P_{II2} < P_{\mathcal{A}2}$ 

Pneumatic spring:

- the amount of the air flowing through the throttling orifice with extra tanks in the air

$$dG_{II2} \cong +\mu S_D \sqrt{2\rho_{J2} (P_{J2} - P_{I12})} dt,$$
 (39)  
- law of energy storage

$$RT_{J_{2}}dG_{I12} - k_{I}H_{I}(T_{I12} - T_{0})dt - C_{V}G_{I12}dT_{I12} - P_{I12}dV_{I12} - C_{V}T_{I12}dG_{I12} + C_{V}T_{J2}dG_{I12} = 0$$
(40)

- the equation of state of the air

 $P_{\Pi 2}dV_{\Pi 2} + V_{\Pi 2}dP_{\Pi 2} - RT_{\Pi 2}dG_{\Pi 2} - RG_{\Pi 2}dT_{\Pi 2} = 0.$  (41) Additional tank:

- the weight balance equation

$$dG_{II2} + dG_{II2} = 0$$
, also  $dG_{II2} = -dG_{II2}$ , (42)

- the law of energy storage

$$RT_{\mathcal{A}\mathcal{D}} dG_{\mathcal{A}\mathcal{D}} - C_V G_{\mathcal{A}\mathcal{D}} dT_{\mathcal{A}\mathcal{D}} - k_2 H_2 (T_{\mathcal{A}\mathcal{D}} - T_0) dt = 0, (43)$$

 $V_{J2}dP_{J2} - RT_{J2}dG_{J2} - RG_{J2}dT_{J2} = 0.$  (44)

Conclusions. The above mathematical model of plane vertical oscillations of the trolley for transporting dangerous cargo, which has a high quality two-stage spring suspension, consists of mechanical systems (10, 11, 14-17),power (2,4,5,8), geometrical (3. 6,7,9,21,28) and thermodynamical (18-20, 22-27, 29-44) equations that define the powered motion of the system during the vibrations that are caused by geometrical irregularities quite hard road profile of given configuration  $\eta = \eta (\xi)$ .

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# Лагутин В.Л. Математическая модель плоских вертикальных колебаний прицепа для транспортировки опасных грузив с использованием пневматических элементов во второй ступени подвешивания

Аннотация. Рассматривается построение математической модели плоских вертикальных колебаний прицепа для транспортирования опасных грузов, который имеет двухступенчатое рессорное подвешивание повышенного качества с использованием пневмоэлементов.

Ключевые слова: взрывоопасный груз, двухступенчатое рессорное подвешивание, колебания.